

CS 240

Data Structures and Algorithms I

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A Generic ArrayStack

```
class ArrayStack<E> implements Stack<E> {  
    public void push(E value) { ... }  
  
    public E pop()  
        throws StackUnderflowException { ... }  
  
    public E top()  
        throws StackUnderflowException { ... }  
  
    public boolean isEmpty() { ... }  
  
    public int size() { ... }  
}
```

Let's play with the file `ArrayStack.java` from the course website

Java API

- For the sake of discussion, we've been implementing stacks by hand
- Java has many data structures included with its libraries
- Because it's so extensive, it's important to be familiar with the Java libraries' APIs
- <http://download.oracle.com/javase/7/docs/api/java/util/Stack.html>

One Final Talking Point...

Q: How efficient are the stack operations?

A: Depends on the implementation!

Let's take a look at our `ArrayStack`:

Operation	Worst-Case Running Time
<code>size</code>	
<code>isEmpty</code>	
<code>top</code>	
<code>pop</code>	
<code>push</code>	

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Let's take a look at our ArrayStack:

Operation	Worst-Case Running Time
size	$O(1)$
isEmpty	
top	
pop	
push	

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Let's take a look at our ArrayStack:

Operation	Worst-Case Running Time
size	$O(1)$
isEmpty	$O(1)$
top	$O(1)$
pop	$O(1)$
push	$O(n)$

Amortized Analysis

- At worst, `push` takes $O(n)$ time to resize the array...
- ... But how often does that happen?
- Idea: average out the cost of n operations performed in sequence

```
public void push(E value) {  
    if (size() == data.length)  
        grow();  
    data[++top] = value;  
}
```

Q: What if `grow()` increases the size of the array by 1?

Q: What if `grow()` **doubles** the size of the array?